

38.3 Given (by 38.68)  $\Delta E = \frac{4\pi}{3} \frac{e^2}{R} \beta^3 \left(\frac{E}{mc^2}\right)^4$ , and  $\beta \approx 1$

$\frac{1}{2}$   
 $\Rightarrow \Delta E = \frac{4\pi}{3} \frac{e^2}{R} \cdot \hbar c \left(\frac{E}{R}\right)$

Note  $\hbar c = 197 \text{ MeV} \cdot \text{fm} = 197 \frac{\text{MeV}}{\text{MeV}} \left( \frac{1.602 \cdot 10^{-13} \text{ kg m}^2/\text{s}^2}{\text{MeV}} \right) \frac{\text{fm} \cdot \text{m}}{10^{15} \text{ fm}}$   
 $= 3.16 \cdot 10^{-26} \text{ J} \cdot \text{m}$

Note  $\frac{e^2}{\hbar c} \approx \frac{1}{137}$

$m = 9.11 \cdot 10^{-31} \text{ kg}$ ,  $c = 3 \cdot 10^8 \text{ m/s} \Rightarrow (mc^2)^4 = 4.52 \cdot 10^{-53} \text{ kg}^4 \text{ m}^3/\text{s}^8$   
 $= 4.52 \cdot 10^{-53} \text{ J}^4$

$\Delta E = \frac{4\pi}{3} \frac{1}{137} \frac{3.16 \cdot 10^{-26} \text{ J} \cdot \text{m}}{4.52 \cdot 10^{-53} \text{ J}^4} \left(\frac{E}{R}\right)$

$= 2.14 \cdot 10^{25} \frac{\text{m}}{\text{J}^3} \left(\frac{E}{R}\right) = 8.85 \cdot 10^{-5} \frac{\text{m}}{\text{GeV}^3} \left(\frac{E}{R}\right)$

Assuming  $R$  is in meters, and  $E$  is in GeV, we can convert  $\Delta E$  to MeV by multiplying by  $10^6$

$\therefore \Delta E(\text{keV}) = 88.5 \text{ keV} \left(\frac{\text{m}}{\text{GeV}^3}\right) \left(\frac{E(\text{GeV})^4}{R(\text{m})}\right)$

... this is an odd problem!