

36.4 Equation 36.9 gives us $\frac{d^2P}{d\omega d\Omega} = \frac{\omega^2 e^2}{4\pi^2 c} \left(\frac{v^2}{c^2} - 1 \right) 2\pi \delta(\omega(1 - \frac{v}{c} \cos\theta))$

$\frac{+2}{2}$

In this case $\mu > 1$, and $\epsilon = 1$, so $n = \sqrt{\epsilon\mu} = \sqrt{\mu}$

$e \rightarrow \frac{c}{\sqrt{\epsilon\mu}} = \frac{c}{n}$, $e \rightarrow \frac{1}{\sqrt{\epsilon}} e = e$

$\therefore \frac{d^2P}{d\omega d\Omega} = \frac{\omega^2 e^2 n}{4\pi^2 c} \left(\frac{v^2 n^2}{c^2} - 1 \right) 2\pi \delta(\omega(1 - \frac{vn}{c} \cos\theta))$

Integrate to get $dP/d\omega$

$\frac{dP}{d\omega} = \frac{e^2 n}{2\pi c} \left(\frac{v^2 n^2}{c^2} - 1 \right) \int d\Omega \omega^2 \delta(\omega(1 - \frac{vn}{c} \cos\theta))$

$d\Omega = \sin\theta d\theta d\phi$ The ϕ -integration is trivial.

$\frac{dP}{d\omega} = \frac{\omega^2 e^2 n}{c} \left(\frac{v^2 n^2}{c^2} - 1 \right) \int \sin\theta d\theta \delta(\omega(1 - \frac{vn}{c} \cos\theta))$

$= \frac{\omega^2 e^2 n}{c} \left(\frac{v^2 n^2}{c^2} - 1 \right) \int d(\cos\theta) \delta(\omega(1 - \frac{vn}{c} \cos\theta))$

The dirac delta's argument is zero when $\cos\theta = \frac{c}{vn\omega}$

$= \frac{\omega^2 e^2 n(\omega)}{c} \left(\frac{v^2 n(\omega)^2}{c^2} - 1 \right) \left[\frac{c}{\omega vn(\omega)} \right]$ when $n(\omega) = \sqrt{\mu} > \frac{c}{v}$

$\therefore \frac{dP}{d\omega} = \frac{e^2 \omega}{v} \left(\frac{v^2 n(\omega)^2}{c^2} - 1 \right) = \omega \frac{e^2 v}{c^2} \left(n(\omega)^2 - \frac{c^2}{v^2} \right)$

Now, $\frac{-dE}{dz} = \frac{-dE}{dt} \frac{dt}{dz} = \frac{-dE}{dt} \frac{1}{v} = \frac{P}{v} = \frac{1}{v} \int_0^\infty d\omega \frac{dP}{d\omega}$

$\Rightarrow \frac{-dE}{dz} = \int d\omega \omega \frac{e^2}{c^2} \left[n^2(\omega) - \frac{c^2}{v^2} \right]$