

32.2

Once again I start with 32.2.5

$$P = \frac{2}{3} \frac{e^2}{c^3} (\ddot{a})^2$$

$\frac{+2.5}{3}$

This is a hooke's law potential, so $F = -kx$, and we are given $k = m\omega_0^2$.
 $\Rightarrow F = ma = -m\omega_0^2 x \Rightarrow a = \omega_0^2 x \downarrow$

$$\boxed{P = \frac{2e^2}{3c^3} (\omega_0^2 \bar{x})^2} \quad \checkmark \text{ where I have time averaged.}$$

For a hooke's law potential, $\bar{V} = \frac{1}{2} k \bar{x}^2 = \frac{1}{2} m \omega_0^2 \bar{x}^2$,
and by the virial theorem, $\bar{V} = \frac{1}{2} E \Rightarrow E = m \omega_0^2 \bar{x}^2 \checkmark$

Since $P = \gamma E$, $\boxed{\gamma = \omega_0^2 \frac{2e^2}{3mc^3}} \checkmark$

We are also given $P = -\frac{dE}{dt}$, so a solution to the ODE is
 $E(t) = E(0)e^{-\gamma t}$.

Thus γ is, again, a characteristic lifetime

For $\omega_0 = 10^{15} \text{ s}^{-1}$

I'll use a He atom (mass: $6.64 \cdot 10^{-27} \text{ kg}$)

Huh? $m = m_e$

To convert to SI units, set $e \rightarrow (4\pi\epsilon_0)^{-1/2} e$

$$\frac{1}{\gamma} = \frac{3mc^3}{2e^2\omega_0^2} \xrightarrow{\text{SI}} \frac{1}{\gamma} = \frac{\sqrt{4\pi\epsilon_0} 3mc^3}{2e^2\omega_0^2}$$

I plugged the numbers in using Mathematica! (see attached)

$$\boxed{\frac{1}{\gamma} \approx 3.7 \cdot 10^{-7} \text{ s}}$$